

Problem x.yz. Delete this text and write theorem statement here. We can draw the sets \mathbb{R} , \mathbb{Q} , \mathbb{I} , \mathbb{Z} , and \mathbb{N} . Let's assume our problem was: Prove that:

$$(\forall x \in \mathbb{N}) \left[\sum_{i=0}^n i = \frac{n(n+1)}{2} \right]$$

Proof. I will induct on n

Base case ($n = 1$): $\sum_{i=0}^1 i = 1 = \frac{1(1+1)}{2} = 1$

Inductive Hypothesis: Assume $\sum_{i=0}^k i = \frac{k(k+1)}{2}$ for some $k \in \mathbb{N}$

Inductive Step: [I must show: $\sum_{i=0}^{k+1} i = \frac{(k+1)(k+2)}{2}$]

$$\begin{aligned} \sum_{i=0}^{k+1} i &= k+1 + \sum_{i=0}^k i && \text{[By definition of series]} \\ &= (k+1) + \frac{k(k+1)}{2} && \text{[By I.H]} \\ &= \frac{(2k+2) + (k^2+k)}{2} \\ &= \frac{k^2 + 3k + 2}{2} \\ &= \frac{(k+1)(k+2)}{2} \end{aligned}$$

\therefore By the principle of induction, the claim holds for all $n \in \mathbb{N}$ ■

Proposition x.yz. Let $n \in \mathbb{Z}$.

Disproof. Blah, blah, blah. I'm so smart. ■