

UNIVERSITÄT  
DUISBURG  
ESSEN

*Open-Minded*

DISSERTATION

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**Thesis name**

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From the Faculty of Physics  
the University of Duisburg-Essen  
approved dissertatio  
to obtain the degree  
Dr. rer. nat.  
from

**M. Sc. Name**  
from Birthplace

Advisor:  
Ph. D. xxx  
Co-advisor:  
Ph. D. yyy

Duisburg, Germany  
20xx



UNIVERSITÄT  
DUISBURG  
ESSEN

*Offen im Denken*

DISSERTATION

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**German Thesis name**

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Von der Fakultät für Physik  
der Universität Duisburg-Essen  
genehmigte Dissertation  
zur Erlangung des Grades  
Dr. rer. nat.  
von

**M. Sc. Name**  
aus Birthplace

Gutachter:  
Ph. D. xxx  
Gutachter:  
Ph. D. yyy

Duisburg, Deutschland  
20xx



*A nice quote ...*



Hiermit versichere ich, die vorliegende Dissertation selbstständig, ohne fremde Hilfe und ohne Benutzung anderer als den angegebenen Quellen angefertigt zu haben. Alle aus fremden Werken direkt oder indirekt übernommenen Stellen sind als solche gekennzeichnet. Die vorliegende Dissertation wurde in keinem anderen Promotionsverfahren eingereicht. Mit dieser Arbeit strebe ich die Erlangung des akademischen Grades Doktor der Naturwissenschaften (Dr. rer. nat.) an.

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Ort, Datum

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Author name (on the line the signature)



# Acknowledgments

Some nice words to everyone ...

Name  
Year



# Abstract

Abstract of the thesis.

**Keywords:** some keywords.



# Zusammenfassung

Abstract of the thesis auf Deutsch.

**Schlüsselwörter:** manche Schlüsselwörter.



# List of publications

Publications



# Author contributions

Contributions



# List of Symbols

## Symbols with Latin letters

Symbol	Denomination	IS Unit	Definition
$E$	Energy	$J$	Eq. (2-1)
$F$	Force	$N$	Eq. (2-2)

## Symbols with Greek letter

Symbol	Denomination	IS Unit	Definition
$\theta$	Tilt angle	1	Eq. (2-3)

## Abbreviations

Abbreviation	Denomination
$1D$	One-dimensional
$2D$	Two-dimensional
$3D$	Three-dimensional
$AFM$	Atomic Force Microscope
$MEB$	Microscopio Electrónico de Barrido
$RANSAC$	Random Sample Consensus
$SEM$	Scanning Electron Microscopy
$STM$	Scanning Tunneling Microscope
$SNR$	Signal-to-Noise Ratio
$SURF$	Speeded-Up Robust Features

**Abbreviation    Denomination**

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*SD*                Standard Deviation

*SAD*              Sum of Absolute Differences

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# 1. Introduction

## 1.1. Section

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.



*Open-Minded*

Figure 1-1.: A nice plot

- First item in a list
- Second item in a list
- Third item in a list
- Fourth item in a list
- Fifth item in a list

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all

letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{i=n} x_i = \frac{x_1 + x_2 + \dots + x_n}{n}$$

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$$\int_0^{\infty} e^{-\alpha x^2} dx = \frac{1}{2} \sqrt{\int_{-\infty}^{\infty} e^{-\alpha x^2} dx} \int_{-\infty}^{\infty} e^{-\alpha y^2} dy = \frac{1}{2} \sqrt{\frac{\pi}{\alpha}}$$

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

$$\sum_{k=0}^{\infty} a_0 q^k = \lim_{n \rightarrow \infty} \sum_{k=0}^n a_0 q^k = \lim_{n \rightarrow \infty} a_0 \frac{1 - q^{n+1}}{1 - q} = \frac{a_0}{1 - q}$$

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

$$x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-p \pm \sqrt{p^2 - 4q}}{2}$$

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected

font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

$$\frac{\partial^2 \Phi}{\partial x^2} + \frac{\partial^2 \Phi}{\partial y^2} + \frac{\partial^2 \Phi}{\partial z^2} = \frac{1}{c^2} \frac{\partial^2 \Phi}{\partial t^2}$$

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

1. First item in a list
2. Second item in a list
3. Third item in a list
4. Fourth item in a list
5. Fifth item in a list

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

**First** item in a list

**Second** item in a list

**Third** item in a list

**Fourth** item in a list

**Fifth** item in a list

## 2. Data sets

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

This is the second paragraph. Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

And after the second paragraph follows the third paragraph. Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

After this fourth paragraph, we start a new paragraph sequence. Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like “Huardest gefburn”? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

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Some citation [1, 4, 3]. Also in [2].

$$E = mc^2 \tag{2-1}$$

and

$$F = ma \tag{2-2}$$

and

$$\theta = \sin^{-1}(x) \tag{2-3}$$

# A. Affine Transformation

An Affine Transformation is any transformation that can be expressed in the form of a matrix multiplication (linear transformation) followed by a vector addition (translation).

The Affine Transformation preserves collinearity (i.e., all points lying on a line initially still lie on a line after transformation) and ratios of distance (e.g., the midpoint of a line segment remains the midpoint after transformation).

Geometric contraction, expansion, dilation, reflection, rotation, shear, similarity transformations, spiral similarities, and translation are affine transformations, as are their combinations.

**Definition 1.** Affine Transformation in 2D space

Consider a point  $\mathbf{x} = (x, y)$ . Affine transformations of  $\mathbf{x}$  are all transforms that can be written

$$\mathbf{x}' = \begin{bmatrix} ax + by + c \\ dx + ey + f \end{bmatrix}$$

where  $a$  through  $f$  are scalars.

**Example 2.** Affine transformations

If  $a, e = 1$ , and  $b, d = 0$ , then we have a pure translation

$$\mathbf{x}' = \begin{bmatrix} x + c \\ y + f \end{bmatrix}$$

If  $b, d = 0$  and  $c, f = 0$  then we have a pure scaling

$$\mathbf{x}' = \begin{bmatrix} ax \\ ey \end{bmatrix}$$

If  $a, e = \cos \theta$ ,  $b = -\sin \theta$ ,  $d = \sin \theta$ , and  $c, f = 0$ , we have a rotation

$$\mathbf{x}' = \begin{bmatrix} x \cos \theta - y \sin \theta \\ x \sin \theta + y \cos \theta \end{bmatrix}$$

Finally, if  $a, e = 1$ , and  $c, f = 0$  we have the shear transform

$$\mathbf{x}' = \begin{bmatrix} x + by \\ y + dx \end{bmatrix}$$

## B. Horizontal Disparity into Heights

The heights of the 3D models are calculated using the tilt of the sample during the image acquisition. Using the reference plane concept, a point in the image located on the reference plane remains at the same position after the tilting. On the other hand, a point above or below the reference plane will have an horizontal displacement.

Having in mind the relation between the points in the two frames of inclination, it is possible to establish the following relation

$$\Delta a + \Delta c = \Delta a' + \Delta c' \rightarrow |\Delta a - \Delta a'| = |\Delta c - \Delta c'| = r \quad (\text{B-1})$$

and finally, changing to the image plane

$$h = \frac{d \cdot p}{2 \sin \left( \frac{\theta}{2} \right)} \quad (\text{B-2})$$

where  $h$  is the height,  $d$  the disparity in microns,  $\theta$  is the total tilt angle and  $p$  the pixel size in sample units (e.g. microns)

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